gap> LoadPackage(« loops »); true n=12 gap> CanonicalCayleyTable([[1,5],[5,1]]); [[1,2],[2,1]] gap> GroupByMultiplicationTable(ct); <group of size 2 with 2 generators> gap> IsCyclic(last); true n=14 gap> CanonicalCayleyTable([[1,3,5],[3,5,1],[5,1,3]]); [[1,2,3],[2,3,1],[3,1,2]] gap> GroupByMultiplicationTable(ct); <group of size 3 with 3 generators> gap> IsCyclic(last); true n=16 gap> CanonicalCayleyTable([[1,3,5,7],[3,7,1,5],[5,1,7,3],[7,5,3,1]]); [[1, 2, 3, 4], [2, 4, 1, 3], [3, 1, 4, 2], [4, 3, 2, 1]] gap> GroupByMultiplicationTable(ct); <group of size 4 with 4 generators> gap> IsCyclic(last); true n=18 gap> CanonicalCayleyTable([[1,5,7],[5,7,1],[7,1,5]]);[[1,2,3],[2,3,1],[3,1,2]] gap> GroupByMultiplicationTable(ct); <group of size 3 with 3 generators> gap> IsCyclic(last); true n=20 gap> CanonicalCayleyTable([[1,3,7,9],[3,9,1,7],[7,1,9,3],[9,7,3,1]]); [[1, 2, 3, 4], [2, 4, 1, 3], [3, 1, 4, 2], [4, 3, 2, 1]] gap> GroupByMultiplicationTable(ct); <group of size 4 with 4 generators> gap> IsCyclic(last); true n=22 gap> CanonicalCayleyTable([[1,3,5,7,9],[3,9,7,1,5],[5,7,3,9,1],[7,1,9,5,3],[9,5,1,3,7]]); [[1, 2, 3, 4, 5], [2, 5, 4, 1, 3], [3, 4, 2, 5, 1], [4, 1, 5, 3, 2], [5, 3, 1, 2, 4]gap> GroupByMultiplicationTable(ct); <group of size 5 with 5 generators> gap> IsCyclic(last); true

n=24 gap> CanonicalCayleyTable([[1,5,7,11],[5,1,11,7],[7,11,1,5],[11,7,5,1]]);[[1,2,3,4],[2,1,4,3], [3,4,1,2],[4,3,2,1]] gap> GroupByMultiplicationTable(ct); <group of size 4 with 4 generators> gap> IsCyclic(last); false

n=26

gap> CanonicalCayleyTable([[1,3,5,7,9,11],[3,9,11,5,1,7],[5,11,1,9,7,3],[7,5,9,3,11,1], [9,1,7,11,3,5],[11,7,3,1,5,9]]); [[1, 2, 3, 4, 5, 6], [2, 5, 6, 3, 1, 4], [3, 6, 1, 5, 4, 2], [4, 3, 5, 2, 6, 1], [5, 1, 4, 6, 2, 3], [6, 4, 2, 1, 3, 5]] gap> GroupByMultiplicationTable(ct); <group of size 6 with 6 generators> gap> IsCyclic(last); true

n=28 gap> CanonicalCayleyTable([[1,3,5,9,11,13],[3,9,13,1,5,11],[5,13,3,11,1,9],[9,1,11,3,13,5], [11,5,1,13,9,3],[13,11,9,5,3,1]]); [[1, 2, 3, 4, 5, 6], [2, 4, 6, 1, 3, 5], [3, 6, 2, 5, 1, 4], [4, 1, 5, 2, 6, 3], [5, 3, 1, 6, 4, 2], [6, 5, 4, 3, 2, 1]] gap> GroupByMultiplicationTable(ct); <group of size 6 with 6 generators> gap> IsCyclic(last); true

n=30

gap> CanonicalCayleyTable([[1,7,11,13],[7,11,13,1],[11,13,1,7],[13,1,7,11]]);[[1, 2, 3, 4], [2, 3, 4, 1], [3, 4, 1, 2], [4, 1, 2, 3]] gap> GroupByMultiplicationTable(ct); <group of size 4 with 4 generators> gap> IsCyclic(last); true

n=32

gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15],[3,9,15,11,5,1,7,13],[5,15,7,3,13,9,1,11], [7,11,3,15,1,13,5,9],[9,5,13,1,15,3,11,7],[11,1,9,13,3,7,15,5],[13,7,1,5,11,15,9,3], [15,13,11,9,7,5,3,1]]); [[1,2,3,4,5,6,7,8],[2,5,8,6,3,1,4,7], [3,8,4,2,7,5,1,6],[4,6,2,8,1,7,3,5], [5,3,7,1,8,2,6,4],[6,1,5,7,2,4,8,3], [7,4,1,3,6,8,5,2],[8,7,6,5,4,3,2,1]] gap> GroupByMultiplicationTable(); <group of size 8 with 8 generators> gap> IsCyclic(last); true n=34 gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11],[3,9,11,5,1,7],[5,11,1,9,7,3],[7,5,9,3,11,1], [9,1,7,11,3,5],[11,7,3,1,5,9]]); [[1,2,3,4,5,6],[2,5,6,3,1,4],[3,6,1,5,4,2], [4,3,5,2,6,1],[5,1,4,6,2,3],[6,4,2,1,3,5]] gap> GroupByMultiplicationTable(); <group of size 6 with 6 generators> gap> IsCyclic(last); true

n=36

gap> ct:=CanonicalCayleyTable([[1,5,7,11,13,17],[5,11,1,17,7,13],[7,1,13,5,17,11],[11,17,5,13,1,7],
[13,7,17,1,11,5],[17,13,11,7,5,1]]);
[[1, 2, 3, 4, 5, 6], [2, 4, 1, 6, 3, 5], [3, 1, 5, 2, 6, 4],
 [4, 6, 2, 5, 1, 3], [5, 3, 6, 1, 4, 2], [6, 5, 4, 3, 2, 1]]
gap> GroupByMultiplicationTable();
<group of size 6 with 6 generators>
gap> IsCyclic(last);
true

n=38

gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17],[3,9,15,17,11,5,1,7,13], [5,15,13,3,7,17,11,1,9],[7,17,3,11,13,1,15,9,5],[9,11,7,13,5,15,3,17,1],[11,5,17,1,15,7,9,13,3],[13,1,11,15,3,9,17,5,7], [15,7,1,9,17,13,5,3,11], [17,13,9,5,1,3,7,11,15]]);[[1, 2, 3, 4, 5, 6, 7, 8, 9], [2, 5, 8, 9, 6, 3, 1, 4, 7], [3, 8, 7, 2, 4, 9, 6, 1, 5], [4, 9, 2, 6, 7, 1, 8, 5, 3], [5, 6, 4, 7, 3, 8, 2, 9, 1], [6, 3, 9, 1, 8, 4, 5, 7, 2], [7, 1, 6, 8, 2, 5, 9, 3, 4], [8, 4, 1, 5, 9, 7, 3, 2, 6], [9, 7, 5, 3, 1, 2, 4, 6, 8]] gap> GroupByMultiplicationTable(ct); <group of size 9 with 9 generators> gap> IsCyclic(last); true n=40 gap> ct:=CanonicalCayleyTable([[1,3,7,9,11,13,17,19],[3,9,19,13,7,1,11,17],[7,19,9,17,3,11,1,13], [9,13,17,1,19,3,7,11],[11,7,3,19,1,17,13,9],[13,1,11,3,17,9,19,7],[17,11,1,7,13,19,9,3],[19,17,13,11,9,7,3,1]]); [[1, 2, 3, 4, 5, 6, 7, 8], [2, 4, 8, 6, 3, 1, 5, 7], [3, 8, 4, 7, 2, 5, 1, 6], [4, 6, 7, 1, 8, 2, 3, 5], [5, 3, 2, 8, 1, 7, 6, 4], [6, 1, 5, 2, 7, 4, 8, 3], [7, 5, 1, 3, 6, 8, 4, 2], [8, 7, 6, 5, 4, 3, 2, 1]] gap> GroupByMultiplicationTable(ct); <group of size 8 with 8 generators> gap> IsCyclic(last); false n=42 gap> ct:=CanonicalCayleyTable([[1,5,11,13,17,19],[5,17,13,19,1,11],[11,13,5,17,19,1], [13,19,17,1,11,5],[17,1,19,11,5,13],[19,11,1,5,13,17]]);

[[1, 2, 3, 4, 5, 6], [2, 5, 4, 6, 1, 3], [3, 4, 2, 5, 6, 1],

[4, 6, 5, 1, 3, 2], [5, 1, 6, 3, 2, 4], [6, 3, 1, 2, 4, 5]]

```
gap> GroupByMultiplicationTable(ct);
<group of size 6 with 6 generators>
gap> IsCyclic(last);
true
```

```
n=44
```

```
gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,13,15,17,19,21],[3,9,15,21,17,5,1,7,13,19],
[5,15,19,9,1,21,13,3,7,17],[7,21,9,5,19,3,17,13,1,15],[9,17,1,19,7,15,3,21,5,13],
[13,5,21,3,15,7,19,1,17,9],[15,1,13,17,3,19,5,9,21,7],[17,7,3,13,21,1,9,19,15,5],
[19,13,7,1,5,17,21,15,9,3],[21,19,17,15,13,9,7,5,3,1]]);
[ [ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 ], [ 2, 5, 7, 10, 8, 3, 1, 4, 6, 9 ],
 [3, 7, 9, 5, 1, 10, 6, 2, 4, 8], [4, 10, 5, 3, 9, 2, 8, 6, 1, 7],
 [5, 8, 1, 9, 4, 7, 2, 10, 3, 6], [6, 3, 10, 2, 7, 4, 9, 1, 8, 5],
 [7, 1, 6, 8, 2, 9, 3, 5, 10, 4], [8, 4, 2, 6, 10, 1, 5, 9, 7, 3],
 [9, 6, 4, 1, 3, 8, 10, 7, 5, 2], [10, 9, 8, 7, 6, 5, 4, 3, 2, 1]]
gap> GroupByMultiplicationTable(ct);
<group of size 10 with 10 generators>
gap> IsCyclic(last);
true
n=46
gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,19,21],[3,9,15,21,19,13,7,1,5,11,17],
[5,15,21,11,1,9,19,17,7,3,13],[7,21,11,3,17,15,1,13,19,5,9],[9,19,1,17,11,7,21,3,15,13,5],
[11,13,9,15,7,17,5,19,3,21,1],[13,7,19,1,21,5,15,11,9,17,3],[15,1,17,13,3,19,11,5,21,9,7],
[17,5,7,19,15,3,9,21,13,1,11],[19,11,3,5,13,21,17,9,1,7,15],[21,17,13,9,5,1,3,7,11,15,19]]);
[ [ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 ], [ 2, 5, 8, 11, 10, 7, 4, 1, 3, 6, 9 ]
  , [3, 8, 11, 6, 1, 5, 10, 9, 4, 2, 7],
 [4, 11, 6, 2, 9, 8, 1, 7, 10, 3, 5], [5, 10, 1, 9, 6, 4, 11, 2, 8, 7, 3]
  , [6, 7, 5, 8, 4, 9, 3, 10, 2, 11, 1],
 [7, 4, 10, 1, 11, 3, 8, 6, 5, 9, 2], [8, 1, 9, 7, 2, 10, 6, 3, 11, 5, 4]
  , [9, 3, 4, 10, 8, 2, 5, 11, 7, 1, 6],
 [10, 6, 2, 3, 7, 11, 9, 5, 1, 4, 8],
 [11, 9, 7, 5, 3, 1, 2, 4, 6, 8, 10]]
gap> GroupByMultiplicationTable(ct);
<group of size 11 with 11 generators>
gap> IsCyclic(last);
true
n=48
gap> ct:=CanonicalCayleyTable([[1,5,7,11,13,17,19,23],[5,23,13,7,17,11,1,19],
[7,13,1,19,5,23,11,17],[11,7,19,23,1,5,17,13],[13,17,5,1,23,19,7,11],[17,11,23,5,19,1,13,7],
[19,1,11,17,7,13,23,5],[23,19,17,13,11,7,5,1]]);
[ [ 1, 2, 3, 4, 5, 6, 7, 8 ], [ 2, 8, 5, 3, 6, 4, 1, 7 ],
 [3, 5, 1, 7, 2, 8, 4, 6], [4, 3, 7, 8, 1, 2, 6, 5],
 [5, 6, 2, 1, 8, 7, 3, 4], [6, 4, 8, 2, 7, 1, 5, 3],
 [7, 1, 4, 6, 3, 5, 8, 2], [8, 7, 6, 5, 4, 3, 2, 1]
gap> GroupByMultiplicationTable(ct);
<group of size 8 with 8 generators>
```

```
gap> IsCyclic(last);
```

```
false
```

ct:=CanonicalCayleyTable([[1,3,7,9,11,13,17,19,21,23],[3,9,21,23,17,11,1,7,13,19], [7,21,1,13,23,9,19,17,3,11],[9,23,13,19,1,17,3,21,11,7],[11,17,23,1,21,7,13,9,19,3], [13,11,9,17,7,19,21,3,23,1],[17,1,19,3,13,21,11,23,7,9],[19,7,17,21,9,3,23,11,1,13], [21,13,3,11,19,23,7,1,9,17],[23,19,11,7,3,1,9,13,17,21]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10], [2, 4, 9, 10, 7, 5, 1, 3, 6, 8], [3, 9, 1, 6, 10, 4, 8, 7, 2, 5], [4, 10, 6, 8, 1, 7, 2, 9, 5, 3], [5, 7, 10, 1, 9, 3, 6, 4, 8, 2], [6, 5, 4, 7, 3, 8, 9, 2, 10, 1], [7, 1, 8, 2, 6, 9, 5, 10, 3, 4], [8, 3, 7, 9, 4, 2, 10, 5, 1, 6], [9, 6, 2, 5, 8, 10, 3, 1, 4, 7], [10, 8, 5, 3, 2, 1, 4, 6, 7, 9]] gap> GroupByMultiplicationTable(ct); <group of size 10 with 10 generators> gap> IsCyclic(last); true n=52 gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,15,17,19,21,23,25],[3,9,15,21,25,19,7,1,5,11,17,23], [5,15,25,17,7,3,23,19,9,1,11,21],[7,21,17,3,11,25,1,15,23,9,5,19],[9,25,7,11,23,5,21,3,15,19,1,17], [11,19,3,25,5,17,9,21,1,23,7,15], [15,7,23,1,21,9,17,5,25,3,19,11], [17,1,19,15,3,21,5,23,11,7,25,9],[19,5,9,23,15,1,25,11,3,17,21,7],[21,11,1,9,19,23,3,7,17,25,15,5],[23,17,11,5,1,7,19,25,21,15,9,3],[25,23,21,19,17,15,11,9,7,5,3,1]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12], [2, 5, 7, 10, 12, 9, 4, 1, 3, 6, 8, 11], [3, 7, 12, 8, 4, 2, 11, 9, 5, 1, 6, 10], [4, 10, 8, 2, 6, 12, 1, 7, 11, 5, 3, 9], [5, 12, 4, 6, 11, 3, 10, 2, 7, 9, 1, 8], [6, 9, 2, 12, 3, 8, 5, 10, 1, 11, 4, 7], [7, 4, 11, 1, 10, 5, 8, 3, 12, 2, 9, 6], [8, 1, 9, 7, 2, 10, 3, 11, 6, 4, 12, 5], [9, 3, 5, 11, 7, 1, 12, 6, 2, 8, 10, 4], [10, 6, 1, 5, 9, 11, 2, 4, 8, 12, 7, 3], [11, 8, 6, 3, 1, 4, 9, 12, 10, 7, 5, 2], [12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]] gap> GroupByMultiplicationTable(last); <group of size 12 with 12 generators> gap> IsCyclic(last); true n=54 gap> ct:=CanonicalCayleyTable([[1,5,7,11,13,17,19,23,25],[5,25,19,1,11,23,13,7,17], [7,19,5,23,17,11,25,1,13],[11,1,23,13,19,25,7,17,5],[13,11,17,19,7,5,23,25,1], [17,23,11,25,5,19,1,13,7], [19,13,25,7,23,1,17,5,11], [23,7,1,17,25,13,5,11,19],[25,17,13,5,1,7,11,19,23]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9], [2, 9, 7, 1, 4, 8, 5, 3, 6], [3, 7, 2, 8, 6, 4, 9, 1, 5], [4, 1, 8, 5, 7, 9, 3, 6, 2], [5, 4, 6, 7, 3, 2, 8, 9, 1], [6, 8, 4, 9, 2, 7, 1, 5, 3], [7, 5, 9, 3, 8, 1, 6, 2, 4], [8, 3, 1, 6, 9, 5, 2, 4, 7], [9, 6, 5, 2, 1, 3, 4, 7, 8]] gap> GroupByMultiplicationTable(last); <group of size 9 with 9 generators>

- gap> IsCyclic(last);
- true

gap> ct:=CanonicalCayleyTable([[1,3,5,9,11,13,15,17,19,23,25,27], [3,9,15,27,23,17,11,5,1,13,19,25],[5,15,25,11,1,9,19,27,17,3,13,23], [9,27,11,25,13,5,23,15,3,17,1,19],[11,23,1,13,9,25,3,19,15,27,5,17], [13,17,9,5,25,1,27,3,23,19,11,15],[15,11,19,23,3,27,1,25,5,9,17,13], [17,5,27,15,19,3,25,9,13,1,23,11],[19,1,17,3,15,23,5,13,25,11,27,9], [23,13,3,17,27,19,9,1,11,25,15,5],[25,19,13,1,5,11,17,23,27,15,9,3], [27,25,23,19,17,15,13,11,9,5,3,1]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12], [2, 4, 7, 12, 10, 8, 5, 3, 1, 6, 9, 11], [3, 7, 11, 5, 1, 4, 9, 12, 8, 2, 6, 10], [4, 12, 5, 11, 6, 3, 10, 7, 2, 8, 1, 9], [5, 10, 1, 6, 4, 11, 2, 9, 7, 12, 3, 8], [6, 8, 4, 3, 11, 1, 12, 2, 10, 9, 5, 7], [7, 5, 9, 10, 2, 12, 1, 11, 3, 4, 8, 6], [8, 3, 12, 7, 9, 2, 11, 4, 6, 1, 10, 5], [9, 1, 8, 2, 7, 10, 3, 6, 11, 5, 12, 4], [10, 6, 2, 8, 12, 9, 4, 1, 5, 11, 7, 3], [11, 9, 6, 1, 3, 5, 8, 10, 12, 7, 4, 2], [12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]] gap> GroupByMultiplicationTable(last); <group of size 12 with 12 generators> gap> IsCyclic(last); false

n=58

gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,19,21,23,25,27], [3,9,15,21,27,25,19,13,7,1,5,11,17,23],[5,15,25,23,13,3,7,17,27,21,11,1,9,19], [7,21,23,9,5,19,25,11,3,17,27,13,1,15],[9,27,13,5,23,17,1,19,21,3,15,25,7,11], [11,25,3,19,17,5,27,9,13,23,1,21,15,7],[13,19,7,25,1,27,5,21,11,15,17,9,23,3], [15,13,17,11,19,9,21,7,23,5,25,3,27,1],[17,7,27,3,21,13,11,23,1,25,9,15,19,5], [19,1,21,17,3,23,15,5,25,13,7,27,11,9],[21,5,11,27,15,1,17,25,9,7,23,19,3,13], [23,11,1,13,25,21,9,3,15,27,19,7,5,17],[25,17,9,1,7,15,23,27,19,11,3,5,13,21], [27,23,19,15,11,7,3,1,5,9,13,17,21,25]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14], [2, 5, 8, 11, 14, 13, 10, 7, 4, 1, 3, 6, 9, 12], [3, 8, 13, 12, 7, 2, 4, 9, 14, 11, 6, 1, 5, 10], [4, 11, 12, 5, 3, 10, 13, 6, 2, 9, 14, 7, 1, 8], [5, 14, 7, 3, 12, 9, 1, 10, 11, 2, 8, 13, 4, 6], [6, 13, 2, 10, 9, 3, 14, 5, 7, 12, 1, 11, 8, 4], [7, 10, 4, 13, 1, 14, 3, 11, 6, 8, 9, 5, 12, 2], [8, 7, 9, 6, 10, 5, 11, 4, 12, 3, 13, 2, 14, 1], [9, 4, 14, 2, 11, 7, 6, 12, 1, 13, 5, 8, 10, 3], [10, 1, 11, 9, 2, 12, 8, 3, 13, 7, 4, 14, 6, 5], [11, 3, 6, 14, 8, 1, 9, 13, 5, 4, 12, 10, 2, 7], [12, 6, 1, 7, 13, 11, 5, 2, 8, 14, 10, 4, 3, 9], [13, 9, 5, 1, 4, 8, 12, 14, 10, 6, 2, 3, 7, 11], [14, 12, 10, 8, 6, 4, 2, 1, 3, 5, 7, 9, 11, 13]] gap> GroupByMultiplicationTable(last); <group of size 14 with 14 generators> gap> IsCyclic(last); true

```
n=60
gap> ct:=CanonicalCayleyTable([[1,7,11,13,17,19,23,29],[7,11,17,29,1,13,19,23],
[11,17,1,23,7,29,13,19],[13,29,23,11,19,7,1,17],[17,1,7,19,11,23,29,13],[19,13,29,7,23,1,17,11],
[23,19,13,1,29,17,11,7],[29,23,19,17,13,11,7,1]]);
[ [ 1, 2, 3, 4, 5, 6, 7, 8 ], [ 2, 3, 5, 8, 1, 4, 6, 7 ],
 [3, 5, 1, 7, 2, 8, 4, 6], [4, 8, 7, 3, 6, 2, 1, 5],
 [5, 1, 2, 6, 3, 7, 8, 4], [6, 4, 8, 2, 7, 1, 5, 3],
 [7, 6, 4, 1, 8, 5, 3, 2], [8, 7, 6, 5, 4, 3, 2, 1]]
gap> GroupByMultiplicationTable(last);
<group of size 8 with 8 generators>
gap> IsCyclic(last);
false
n=62
gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,19,21,23,25,27,29],
[3,9,15,21,27,29,23,17,11,5,1,7,13,19,25],[5,15,25,27,17,7,3,13,23,29,19,9,1,11,21],
[7,21,27,13,1,15,29,19,5,9,23,25,11,3,17],[9,27,17,1,19,25,7,11,29,15,3,21,23,5,13],
[11,29,7,15,25,3,19,21,1,23,17,5,27,13,9],[13,23,3,29,7,19,17,9,27,1,25,11,15,21,5],
[15,17,13,19,11,21,9,23,7,25,5,27,3,29,1],[17,11,23,5,29,1,27,7,21,13,15,19,9,25,3],
[19,5,29,9,15,23,1,25,13,11,27,3,21,17,7],[21,1,19,23,3,17,25,5,15,27,7,13,29,9,11],
[23,7,9,25,21,5,11,27,19,3,13,29,17,1,15],[25,13,1,11,23,27,15,3,9,21,29,17,5,7,19],
[27,19,11,3,5,13,21,29,25,17,9,1,7,15,23],[29,25,21,17,13,9,5,1,3,7,11,15,19,23,27]]);
[ [ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15 ],
 [2, 5, 8, 11, 14, 15, 12, 9, 6, 3, 1, 4, 7, 10, 13],
 [3, 8, 13, 14, 9, 4, 2, 7, 12, 15, 10, 5, 1, 6, 11],
 [4, 11, 14, 7, 1, 8, 15, 10, 3, 5, 12, 13, 6, 2, 9],
 [5, 14, 9, 1, 10, 13, 4, 6, 15, 8, 2, 11, 12, 3, 7],
 [6, 15, 4, 8, 13, 2, 10, 11, 1, 12, 9, 3, 14, 7, 5],
 [7, 12, 2, 15, 4, 10, 9, 5, 14, 1, 13, 6, 8, 11, 3],
 [8, 9, 7, 10, 6, 11, 5, 12, 4, 13, 3, 14, 2, 15, 1],
 [9, 6, 12, 3, 15, 1, 14, 4, 11, 7, 8, 10, 5, 13, 2],
 [10, 3, 15, 5, 8, 12, 1, 13, 7, 6, 14, 2, 11, 9, 4],
 [11, 1, 10, 12, 2, 9, 13, 3, 8, 14, 4, 7, 15, 5, 6],
 [12, 4, 5, 13, 11, 3, 6, 14, 10, 2, 7, 15, 9, 1, 8],
 [13, 7, 1, 6, 12, 14, 8, 2, 5, 11, 15, 9, 3, 4, 10],
 [14, 10, 6, 2, 3, 7, 11, 15, 13, 9, 5, 1, 4, 8, 12],
 [15, 13, 11, 9, 7, 5, 3, 1, 2, 4, 6, 8, 10, 12, 14]]
```

gap> GroupByMultiplicationTable(last);

<group of size 15 with 15 generators>

gap> IsCyclic(last);

true

n=64

gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,19,21,23,25,27,29,31], [3,9,15,21,27,31,25,19,13,7,1,5,11,17,23,29],[5,15,25,29,19,9,1,11,21,31,23,13,3,7,17,27], [7,21,29,15,1,13,27,23,9,5,19,31,17,3,11,25],[9,27,19,1,17,29,11,7,25,21,3,15,31,13,5,23], [11,31,9,13,29,7,15,27,5,17,25,3,19,23,1,21],[13,25,1,27,11,15,23,3,29,9,17,21,5,31,7,19], [15,19,11,23,7,27,3,31,1,29,5,25,9,21,13,17],[17,13,21,9,25,5,29,1,31,3,27,7,23,11,19,15], [19,7,31,5,21,17,9,29,3,23,15,11,27,1,25,13],[21,1,23,19,3,25,17,5,27,15,7,29,13,9,31,11], [23,5,13,31,15,3,21,25,7,11,29,17,1,19,27,9],[25,11,3,17,31,19,59,23,27,13,1,15,29,21,7], [27,17,7,3,13,23,31,21,11,1,9,19,29,25,15,5],[29,23,17,11,5,1,7,13,19,25,31,27,21,15,9,3],

[31,29,27,25,23,21,19,17,15,13,11,9,7,5,3,1]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16], [2, 5, 8, 11, 14, 16, 13, 10, 7, 4, 1, 3, 6, 9, 12, 15], [3, 8, 13, 15, 10, 5, 1, 6, 11, 16, 12, 7, 2, 4, 9, 14], [4, 11, 15, 8, 1, 7, 14, 12, 5, 3, 10, 16, 9, 2, 6, 13], [5, 14, 10, 1, 9, 15, 6, 4, 13, 11, 2, 8, 16, 7, 3, 12], [6, 16, 5, 7, 15, 4, 8, 14, 3, 9, 13, 2, 10, 12, 1, 11], [7, 13, 1, 14, 6, 8, 12, 2, 15, 5, 9, 11, 3, 16, 4, 10], [8, 10, 6, 12, 4, 14, 2, 16, 1, 15, 3, 13, 5, 11, 7, 9], [9, 7, 11, 5, 13, 3, 15, 1, 16, 2, 14, 4, 12, 6, 10, 8], [10, 4, 16, 3, 11, 9, 5, 15, 2, 12, 8, 6, 14, 1, 13, 7], [11, 1, 12, 10, 2, 13, 9, 3, 14, 8, 4, 15, 7, 5, 16, 6], [12, 3, 7, 16, 8, 2, 11, 13, 4, 6, 15, 9, 1, 10, 14, 5], [13, 6, 2, 9, 16, 10, 3, 5, 12, 14, 7, 1, 8, 15, 11, 4], [14, 9, 4, 2, 7, 12, 16, 11, 6, 1, 5, 10, 15, 13, 8, 3], [15, 12, 9, 6, 3, 1, 4, 7, 10, 13, 16, 14, 11, 8, 5, 2], [16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]] gap> GroupByMultiplicationTable(last); <group of size 16 with 16 generators> gap> IsCyclic(last); true

n=66

gap> ct:=CanonicalCayleyTable([[1,5,7,13,17,19,23,25,29,31],[5,25,31,1,19,29,17,7,13,23], [7,31,17,25,13,1,29,23,5,19],[13,1,25,29,23,17,31,5,19,7],[17,19,13,23,25,7,5,29,31,1], [19,29,1,17,7,31,25,13,23,5],[23,17,29,31,5,25,1,19,7,13],[25,7,23,5,29,13,19,31,1,17], [29,13,5,19,31,23,7,1,17,25],[31,23,19,7,1,5,13,17,25,29]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10], [2, 8, 10, 1, 6, 9, 5, 3, 4, 7], [3, 10, 5, 8, 4, 1, 9, 7, 2, 6], [4, 1, 8, 9, 7, 5, 10, 2, 6, 3], [5, 6, 4, 7, 8, 3, 2, 9, 10, 1], [6, 9, 1, 5, 3, 10, 8, 4, 7, 2], [7, 5, 9, 10, 2, 8, 1, 6, 3, 4], [8, 3, 7, 2, 9, 4, 6, 10, 1, 5], [9, 4, 2, 6, 10, 7, 3, 1, 5, 8], [10, 7, 6, 3, 1, 2, 4, 5, 8, 9]] gap> GroupByMultiplicationTable(last); <group of size 10 with 10 generators> gap> IsCyclic(last); true

n=68

gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,19,21,23,25,27,29,31,33], [3,9,15,21,27,33,29,23,11,5,1,7,13,19,25,31],[5,15,25,33,23,13,3,7,27,31,21,11,1,9,19,29], [7,21,33,19,5,9,23,31,3,11,25,29,15,1,13,27],[9,27,23,5,13,31,19,1,33,15,3,21,29,11,7,25], [11,33,13,9,31,15,7,29,5,27,19,3,25,21,1,23],[13,29,3,23,19,7,33,9,25,1,27,15,11,31,5,21], [15,23,7,31,1,29,9,21,13,25,5,33,3,27,11,19],[19,11,27,3,33,5,25,13,21,9,29,1,31,7,23,15], [21,5,31,11,15,27,1,25,9,33,7,19,23,3,29,13],[23,1,21,25,3,19,27,5,29,7,15,31,9,13,33,11], [25,7,11,29,21,3,15,33,1,19,31,13,5,23,27,9],[27,13,1,15,29,25,11,3,31,23,9,5,19,33,21,7], [29,19,9,1,11,21,31,27,7,3,13,23,33,25,15,5],[31,25,19,13,7,1,5,11,23,29,33,27,21,15,9,3], [33,31,29,27,25,23,21,19,15,13,11,9,7,5,3,1]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16],

[2, 5, 8, 10, 13, 16, 14, 11, 6, 3, 1, 4, 7, 9, 12, 15],

[3, 8, 12, 16, 11, 7, 2, 4, 13, 15, 10, 6, 1, 5, 9, 14],

[4, 10, 16, 9, 3, 5, 11, 15, 2, 6, 12, 14, 8, 1, 7, 13],

[5, 13, 11, 3, 7, 15, 9, 1, 16, 8, 2, 10, 14, 6, 4, 12],

[6, 16, 7, 5, 15, 8, 4, 14, 3, 13, 9, 2, 12, 10, 1, 11], [7, 14, 2, 11, 9, 4, 16, 5, 12, 1, 13, 8, 6, 15, 3, 10], [8, 11, 4, 15, 1, 14, 5, 10, 7, 12, 3, 16, 2, 13, 6, 9], [9, 6, 13, 2, 16, 3, 12, 7, 10, 5, 14, 1, 15, 4, 11, 8], [10, 3, 15, 6, 8, 13, 1, 12, 5, 16, 4, 9, 11, 2, 14, 7], [11, 1, 10, 12, 2, 9, 13, 3, 14, 4, 8, 15, 5, 7, 16, 6], [12, 4, 6, 14, 10, 2, 8, 16, 1, 9, 15, 7, 3, 11, 13, 5], [13, 7, 1, 8, 14, 12, 6, 2, 15, 11, 5, 3, 9, 16, 10, 4], [14, 9, 5, 1, 6, 10, 15, 13, 4, 2, 7, 11, 16, 12, 8, 3], [15, 12, 9, 7, 4, 1, 3, 6, 11, 14, 16, 13, 10, 8, 5, 2], [16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]] gap> GroupByMultiplicationTable(last); <group of size 16 with 16 generators> gap> IsCyclic(last); true

n=70

gap> ct:=CanonicalCayleyTable([[1,3,9,11,13,17,19,23,27,29,31,33], [3,9,27,33,31,19,13,1,11,17,23,29],[9,27,11,29,23,13,31,3,33,19,1,17], [11,33,29,19,3,23,1,27,17,31,9,13],[13,31,23,3,29,11,33,19,1,27,17,9], [17,19,13,23,11,9,27,29,31,3,33,1],[19,13,31,1,33,27,11,17,23,9,29,3], [23,1,3,27,19,29,17,31,9,33,13,11],[27,11,33,17,1,31,23,9,29,13,3,19], [29,17,19,31,27,3,9,33,13,1,11,23],[31,23,1,9,17,33,29,13,3,11,19,27], [33,29,17,13,9,1,3,11,19,23,27,31]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12], [2, 3, 9, 12, 11, 7, 5, 1, 4, 6, 8, 10], [3, 9, 4, 10, 8, 5, 11, 2, 12, 7, 1, 6], [4, 12, 10, 7, 2, 8, 1, 9, 6, 11, 3, 5], [5, 11, 8, 2, 10, 4, 12, 7, 1, 9, 6, 3], [6, 7, 5, 8, 4, 3, 9, 10, 11, 2, 12, 1], [7, 5, 11, 1, 12, 9, 4, 6, 8, 3, 10, 2], [8, 1, 2, 9, 7, 10, 6, 11, 3, 12, 5, 4], [9, 4, 12, 6, 1, 11, 8, 3, 10, 5, 2, 7], [10, 6, 7, 11, 9, 2, 3, 12, 5, 1, 4, 8], [11, 8, 1, 3, 6, 12, 10, 5, 2, 4, 7, 9], [12, 10, 6, 5, 3, 1, 2, 4, 7, 8, 9, 11]] gap> GroupByMultiplicationTable(last); <group of size 12 with 12 generators> gap> IsCvclic(last); true n=72 gap> ct:=CanonicalCayleyTable([[1,5,7,11,13,17,19,23,25,29,31,35], [5,25,35,17,7,13,23,29,19,1,11,31],[7,35,23,5,19,25,11,17,31,13,1,29], [11,17,5,23,1,29,7,35,13,31,19,25],[13,7,19,1,25,5,31,11,35,17,29,23],[17,13,25,29,5,1,35,31,7,11,23,19],[19,23,11,7,31,35,1,5,29,25,13,17], [23,29,17,35,11,31,5,25,1,19,7,13],[25,19,31,13,35,7,29,1,23,5,17,11],

[29,1,13,31,17,11,25,19,5,23,35,7],[31,11,1,19,29,23,13,7,17,35,25,5], [35,31,29,25,23,19,17,13,11,7,5,1]]);

[[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12],

[2,9,12,6,3,5,8,10,7,1,4,11],

[3, 12, 8, 2, 7, 9, 4, 6, 11, 5, 1, 10],

[4, 6, 2, 8, 1, 10, 3, 12, 5, 11, 7, 9], [5, 3, 7, 1, 9, 2, 11, 4, 12, 6, 10, 8], [6, 5, 9, 10, 2, 1, 12, 11, 3, 4, 8, 7], [7, 8, 4, 3, 11, 12, 1, 2, 10, 9, 5, 6], [8, 10, 6, 12, 4, 11, 2, 9, 1, 7, 3, 5], [9, 7, 11, 5, 12, 3, 10, 1, 8, 2, 6, 4], [10, 1, 5, 11, 6, 4, 9, 7, 2, 8, 12, 3], [11, 4, 1, 7, 10, 8, 5, 3, 6, 12, 9, 2], [12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]] gap> GroupByMultiplicationTable(last); <group of size 12 with 12 generators> gap> IsCyclic(last); false

n=74

gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,19,21,23,25,27,29,31,33,35], [3,9,15,21,27,33,35,29,23,17,11,5,1,7,13,19,25,31], [5,15,25,35,29,19,9,1,11,21,31,33,23,13,3,7,17,27], [7,21,35,25,11,3,17,31,29,15,1,13,27,33,19,5,9,23], [9,27,29,11,7,25,31,13,5,23,33,15,3,21,35,17,1,19], [11,33,19,3,25,27,5,17,35,13,9,31,21,1,23,29,7,15], [13,35,9,17,31,5,21,27,1,25,23,3,29,19,7,33,15,11], [15,29,1,31,13,17,27,3,33,11,19,25,5,35,9,21,23,7], [17,23,11,29,5,35,1,33,7,27,13,21,19,15,25,9,31,3], [19,17,21,15,23,13,25,11,27,9,29,7,31,5,33,3,35,1], [21,11,31,1,33,9,23,19,13,29,3,35,7,25,17,15,27,5], [23,5,33,13,15,31,3,25,21,7,35,11,17,29,1,27,19,9], [25,1,23,27,3,21,29,5,19,31,7,17,33,9,15,35,11,13], [27,7,13,33,21,1,19,35,15,5,25,29,9,11,31,23,3,17], [29,13,3,19,35,23,7,9,25,33,17,1,15,31,27,11,5,21], [31,19,7,5,17,29,33,21,9,3,15,27,35,23,11,1,13,25], [33,25,17,9,1,7,15,23,31,35,27,19,11,3,5,13,21,29], [35,31,27,23,19,15,11,7,3,1,5,9,13,17,21,25,29,33]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18], [2, 5, 8, 11, 14, 17, 18, 15, 12, 9, 6, 3, 1, 4, 7, 10, 13, 16], [3, 8, 13, 18, 15, 10, 5, 1, 6, 11, 16, 17, 12, 7, 2, 4, 9, 14], [4, 11, 18, 13, 6, 2, 9, 16, 15, 8, 1, 7, 14, 17, 10, 3, 5, 12], [5, 14, 15, 6, 4, 13, 16, 7, 3, 12, 17, 8, 2, 11, 18, 9, 1, 10], [6, 17, 10, 2, 13, 14, 3, 9, 18, 7, 5, 16, 11, 1, 12, 15, 4, 8], [7, 18, 5, 9, 16, 3, 11, 14, 1, 13, 12, 2, 15, 10, 4, 17, 8, 6], [8, 15, 1, 16, 7, 9, 14, 2, 17, 6, 10, 13, 3, 18, 5, 11, 12, 4], [9, 12, 6, 15, 3, 18, 1, 17, 4, 14, 7, 11, 10, 8, 13, 5, 16, 2], [10, 9, 11, 8, 12, 7, 13, 6, 14, 5, 15, 4, 16, 3, 17, 2, 18, 1], [11, 6, 16, 1, 17, 5, 12, 10, 7, 15, 2, 18, 4, 13, 9, 8, 14, 3], [12, 3, 17, 7, 8, 16, 2, 13, 11, 4, 18, 6, 9, 15, 1, 14, 10, 5], [13, 1, 12, 14, 2, 11, 15, 3, 10, 16, 4, 9, 17, 5, 8, 18, 6, 7], [14, 4, 7, 17, 11, 1, 10, 18, 8, 3, 13, 15, 5, 6, 16, 12, 2, 9], [15, 7, 2, 10, 18, 12, 4, 5, 13, 17, 9, 1, 8, 16, 14, 6, 3, 11], [16, 10, 4, 3, 9, 15, 17, 11, 5, 2, 8, 14, 18, 12, 6, 1, 7, 13], [17, 13, 9, 5, 1, 4, 8, 12, 16, 18, 14, 10, 6, 2, 3, 7, 11, 15], [18, 16, 14, 12, 10, 8, 6, 4, 2, 1, 3, 5, 7, 9, 11, 13, 15, 17]] gap> GroupByMultiplicationTable(last);

<group of size 18 with 18 generators> gap> IsCyclic(last); true

n=76

gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,21,23,25,27,29,31,33,35,37], [3,9,15,21,27,33,37,31,25,13,7,1,5,11,17,23,29,35], [5,15,25,35,31,21,11,1,9,29,37,27,17,7,3,13,23,33], [7,21,35,27,13,1,15,29,33,5,9,23,37,25,11,3,17,31], [9,27,31,13,5,23,35,17,1,37,21,3,15,33,25,7,11,29], [11,33,21,1,23,31,9,13,35,3,25,29,7,15,37,17,5,27], [13,37,11,15,35,9,17,33,7,31,5,21,29,3,23,27,1,25], [15,31,1,29,17,13,33,3,27,11,35,5,25,21,9,37,7,23], [17,25,9,33,1,35,7,27,15,23,11,31,3,37,5,29,13,21], [21,13,29,5,37,3,31,11,23,15,27,7,35,1,33,9,25,17], [23,7,37,9,21,25,5,35,11,27,3,33,13,17,29,1,31,15], [25,1,27,23,3,29,21,5,31,7,33,17,9,35,15,11,37,13], [27,5,17,37,15,7,29,25,3,35,13,9,31,23,1,21,33,11], [29,11,7,25,33,15,3,21,37,1,17,35,23,5,13,31,27,9], [31,17,3,11,25,37,23,9,5,33,29,15,1,13,27,35,21,7], [33,23,13,3,7,17,27,37,29,9,1,11,21,31,35,25,15,5], [35,29,23,17,11,5,1,7,13,25,31,37,33,27,21,15,9,3], [37, 35, 33, 31, 29, 27, 25, 23, 21, 17, 15, 13, 11, 9, 7, 5, 3, 1]]);[[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18], [2, 5, 8, 10, 13, 16, 18, 15, 12, 7, 4, 1, 3, 6, 9, 11, 14, 17], [3, 8, 12, 17, 15, 10, 6, 1, 5, 14, 18, 13, 9, 4, 2, 7, 11, 16], [4, 10, 17, 13, 7, 1, 8, 14, 16, 3, 5, 11, 18, 12, 6, 2, 9, 15], [5, 13, 15, 7, 3, 11, 17, 9, 1, 18, 10, 2, 8, 16, 12, 4, 6, 14], [6, 16, 10, 1, 11, 15, 5, 7, 17, 2, 12, 14, 4, 8, 18, 9, 3, 13], [7, 18, 6, 8, 17, 5, 9, 16, 4, 15, 3, 10, 14, 2, 11, 13, 1, 12], [8, 15, 1, 14, 9, 7, 16, 2, 13, 6, 17, 3, 12, 10, 5, 18, 4, 11], [9, 12, 5, 16, 1, 17, 4, 13, 8, 11, 6, 15, 2, 18, 3, 14, 7, 10], [10, 7, 14, 3, 18, 2, 15, 6, 11, 8, 13, 4, 17, 1, 16, 5, 12, 9], [11, 4, 18, 5, 10, 12, 3, 17, 6, 13, 2, 16, 7, 9, 14, 1, 15, 8], [12, 1, 13, 11, 2, 14, 10, 3, 15, 4, 16, 9, 5, 17, 8, 6, 18, 7], [13, 3, 9, 18, 8, 4, 14, 12, 2, 17, 7, 5, 15, 11, 1, 10, 16, 6], [14, 6, 4, 12, 16, 8, 2, 10, 18, 1, 9, 17, 11, 3, 7, 15, 13, 5], [15, 9, 2, 6, 12, 18, 11, 5, 3, 16, 14, 8, 1, 7, 13, 17, 10, 4], [16, 11, 7, 2, 4, 9, 13, 18, 14, 5, 1, 6, 10, 15, 17, 12, 8, 3], [17, 14, 11, 9, 6, 3, 1, 4, 7, 12, 15, 18, 16, 13, 10, 8, 5, 2], [18, 17, 16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]] gap> GroupByMultiplicationTable(last); <group of size 18 with 18 generators> gap> IsCyclic(last); true

n=78

gap> ct:=CanonicalCayleyTable([[1,5,7,11,17,19,23,25,29,31,35,37], [5,25,35,23,7,17,37,31,11,1,19,29],[7,35,29,1,37,23,5,19,31,17,11,25], [11,23,1,35,31,25,19,37,7,29,5,17],[17,7,37,31,23,11,1,35,25,19,29,5], [19,17,23,25,11,29,31,7,5,35,37,1],[23,37,5,19,1,31,17,29,35,11,25,7],

```
[25,31,19,37,35,7,29,1,23,5,17,11],[29,11,31,7,25,5,35,23,17,37,1,19],
[31,1,17,29,19,35,11,5,37,25,7,23],[35,19,11,5,29,37,25,17,1,7,23,31],
[37,29,25,17,5,1,7,11,19,23,31,35]]);
[ [ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12 ],
 [2, 8, 11, 7, 3, 5, 12, 10, 4, 1, 6, 9],
 [3, 11, 9, 1, 12, 7, 2, 6, 10, 5, 4, 8],
 [4, 7, 1, 11, 10, 8, 6, 12, 3, 9, 2, 5],
 [5, 3, 12, 10, 7, 4, 1, 11, 8, 6, 9, 2],
 [6, 5, 7, 8, 4, 9, 10, 3, 2, 11, 12, 1],
 [7, 12, 2, 6, 1, 10, 5, 9, 11, 4, 8, 3],
 [8, 10, 6, 12, 11, 3, 9, 1, 7, 2, 5, 4],
 [9, 4, 10, 3, 8, 2, 11, 7, 5, 12, 1, 6],
 [10, 1, 5, 9, 6, 11, 4, 2, 12, 8, 3, 7],
 [11, 6, 4, 2, 9, 12, 8, 5, 1, 3, 7, 10],
 [12, 9, 8, 5, 2, 1, 3, 4, 6, 7, 10, 11]]
gap> GroupByMultiplicationTable(last);
<group of size 12 with 12 generators>
gap> IsCyclic(last);
true
```

```
gap> ct:=CanonicalCayleyTable([[1,3,7,9,11,13,17,19,21,23,27,29,31,33,37,39],
[3,9,21,27,33,39,29,23,17,11,1,7,13,19,31,37],[7,21,31,17,3,11,39,27,13,1,29,37,23,9,19,33],
[9,27,17,1,19,37,7,11,29,33,3,21,39,23,13,31],[11,33,3,19,39,17,27,31,9,13,23,1,21,37,7,29],
[13,39,11,37,17,9,19,7,33,21,31,23,3,29,1,27],[17,29,39,7,27,19,31,3,37,9,21,13,33,1,11,23],
[19,23,27,11,31,7,3,39,1,37,33,9,29,13,17,21],[21,17,13,29,9,33,37,1,39,3,7,31,11,27,23,19],
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 [16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]]
gap> GroupByMultiplicationTable(last);
<group of size 16 with 16 generators>
gap> IsCyclic(last);
false
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gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,19,21,23,25,27,29,31,33,35,37,39], [3,9,15,21,27,33,39,37,31,25,19,13,7,1,5,11,17,23,29,35], [5,15,25,35,37,27,17,7,3,13,23,33,39,29,19,9,1,11,21,31], [7,21,35,33,19,5,9,23,37,31,17,3,11,25,39,29,15,1,13,27], [9,27,37,19,1,17,35,29,11,7,25,39,21,3,15,33,31,13,5,23], [11,33,27,5,17,39,21,1,23,37,15,7,29,31,9,13,35,25,3,19], [13,39,17,9,35,21,5,31,25,1,27,29,3,23,33,7,19,37,11,15], [15,37,7,23,29,1,31,21,9,39,13,17,35,5,25,27,3,33,19,11], [17,31,3,37,11,23,25,9,39,5,29,19,15,33,1,35,13,21,27,7], [19,25,13,31,7,37,1,39,5,33,11,27,17,21,23,15,29,9,35,3], [21,19,23,17,25,15,27,13,29,11,31,9,33,7,35,5,37,3,39,1], [23,13,33,3,39,7,29,17,19,27,9,37,1,35,11,25,21,15,31,5], [25,7,39,11,21,29,3,35,15,17,33,1,31,19,13,37,5,27,23,9], [27,1,29,25,3,31,23,5,33,21,7,35,19,9,37,17,11,39,15,13], [29,5,19,39,15,9,33,25,1,23,35,11,13,37,21,3,27,31,7,17], [31,11,9,29,33,13,7,27,35,15,5,25,37,17,3,23,39,19,1,21], [33,17,1,15,31,35,19,3,13,29,37,21,5,11,27,39,23,7,9,25], [35,23,11,1,13,25,37,33,21,9,3,15,27,39,31,19,7,5,17,29], [37,29,21,13,5,3,11,19,27,35,39,31,23,15,7,1,9,17,25,33], [39,35,31,27,23,19,15,11,7,3,1,5,9,13,17,21,25,29,33,37]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20], [2, 5, 8, 11, 14, 17, 20, 19, 16, 13, 10, 7, 4, 1, 3, 6, 9, 12, 15, 18], [3, 8, 13, 18, 19, 14, 9, 4, 2, 7, 12, 17, 20, 15, 10, 5, 1, 6, 11, 16], [4, 11, 18, 17, 10, 3, 5, 12, 19, 16, 9, 2, 6, 13, 20, 15, 8, 1, 7, 14], [5, 14, 19, 10, 1, 9, 18, 15, 6, 4, 13, 20, 11, 2, 8, 17, 16, 7, 3, 12], [6, 17, 14, 3, 9, 20, 11, 1, 12, 19, 8, 4, 15, 16, 5, 7, 18, 13, 2, 10], [7, 20, 9, 5, 18, 11, 3, 16, 13, 1, 14, 15, 2, 12, 17, 4, 10, 19, 6, 8], [8, 19, 4, 12, 15, 1, 16, 11, 5, 20, 7, 9, 18, 3, 13, 14, 2, 17, 10, 6], [9, 16, 2, 19, 6, 12, 13, 5, 20, 3, 15, 10, 8, 17, 1, 18, 7, 11, 14, 4], [10, 13, 7, 16, 4, 19, 1, 20, 3, 17, 6, 14, 9, 11, 12, 8, 15, 5, 18, 2], [11, 10, 12, 9, 13, 8, 14, 7, 15, 6, 16, 5, 17, 4, 18, 3, 19, 2, 20, 1], [12, 7, 17, 2, 20, 4, 15, 9, 10, 14, 5, 19, 1, 18, 6, 13, 11, 8, 16, 3], [13, 4, 20, 6, 11, 15, 2, 18, 8, 9, 17, 1, 16, 10, 7, 19, 3, 14, 12, 5], [14, 1, 15, 13, 2, 16, 12, 3, 17, 11, 4, 18, 10, 5, 19, 9, 6, 20, 8, 7], [15, 3, 10, 20, 8, 5, 17, 13, 1, 12, 18, 6, 7, 19, 11, 2, 14, 16, 4, 9], [16, 6, 5, 15, 17, 7, 4, 14, 18, 8, 3, 13, 19, 9, 2, 12, 20, 10, 1, 11], [17, 9, 1, 8, 16, 18, 10, 2, 7, 15, 19, 11, 3, 6, 14, 20, 12, 4, 5, 13], [18, 12, 6, 1, 7, 13, 19, 17, 11, 5, 2, 8, 14, 20, 16, 10, 4, 3, 9, 15], [19, 15, 11, 7, 3, 2, 6, 10, 14, 18, 20, 16, 12, 8, 4, 1, 5, 9, 13, 17], [20, 18, 16, 14, 12, 10, 8, 6, 4, 2, 1, 3, 5, 7, 9, 11, 13, 15, 17, 19]] gap> GroupByMultiplicationTable(last); <group of size 20 with 20 generators> gap> IsCyclic(last); true

n=84

gap> ct:=CanonicalCayleyTable([[1,5,11,13,17,19,23,25,29,31,37,41], [5,25,29,19,1,11,31,41,23,13,17,37],[11,29,37,25,19,41,1,23,17,5,13,31], [13,19,25,1,31,5,37,11,41,17,23,29],[17,1,19,31,37,13,29,5,11,23,41,25], [19,11,41,5,13,25,17,29,37,1,31,23],[23,31,1,37,29,17,25,13,5,41,11,19], [25,41,23,11,5,29,13,37,31,19,1,17],[29,23,17,41,11,37,5,31,1,25,19,13], [31,13,5,17,23,1,41,19,25,37,29,11],[37,17,13,23,41,31,11,1,19,29,25,5],

```
[41,37,31,29,25,23,19,17,13,11,5,1]]);
[ [ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12 ],
 [2, 8, 9, 6, 1, 3, 10, 12, 7, 4, 5, 11],
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 [12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]]
gap> GroupByMultiplicationTable(last);
<group of size 12 with 12 generators>
gap> IsCyclic(last);
false
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gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,19,21,23,25,27,29,31,33,35,37,39,41], [3,9,15,21,27,33,39,41,35,29,23,17,11,5,1,7,13,19,25,31,37], [5,15,25,35,41,31,21,11,1,9,19,29,39,37,27,17,7,3,13,23,33], [7,21,35,37,23,9,5,19,33,39,25,11,3,17,31,41,27,13,1,15,29], [9,27,41,23,5,13,31,37,19,1,17,35,33,15,3,21,39,29,11,7,25], [11,33,31,9,13,35,29,7,15,37,27,5,17,39,25,3,19,41,23,1,21], [13,39,21,5,31,29,3,23,37,11,15,41,19,7,33,27,1,25,35,9,17], [15,41,11,19,37,7,23,33,3,27,29,1,31,25,5,35,21,9,39,17,13], [17,35,1,33,19,15,37,3,31,21,13,39,5,29,23,11,41,7,27,25,9], [19,29,9,39,1,37,11,27,21,17,31,7,41,3,35,13,25,23,15,33,5], [21,23,19,25,17,27,15,29,13,31,11,33,9,35,7,37,5,39,3,41,1], [23,17,29,11,35,5,41,1,39,7,33,13,27,19,21,25,15,31,9,37,3], [25,11,39,3,33,17,19,31,5,41,9,27,23,13,37,1,35,15,21,29,7], [27,5,37,17,15,39,7,25,29,3,35,19,13,41,9,23,31,1,33,21,11], [29,1,27,31,3,25,33,5,23,35,7,21,37,9,19,39,11,17,41,13,15], [31,7,17,41,21,3,27,35,11,13,37,25,1,23,39,15,9,33,29,5,19], [33,13,7,27,39,19,1,21,41,25,5,15,35,31,11,9,29,37,17,3,23], [35,19,3,13,29,41,25,9,7,23,39,31,15,1,17,33,37,21,5,11,27], [37,25,13,1,11,23,35,39,27,15,3,9,21,33,41,29,17,5,7,19,31], [39,31,23,15,7,1,9,17,25,33,41,37,29,21,13,5,3,11,19,27,35], [41,37,33,29,25,21,17,13,9,5,1,3,7,11,15,19,23,27,31,35,39]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21], [2, 5, 8, 11, 14, 17, 20, 21, 18, 15, 12, 9, 6, 3, 1, 4, 7, 10, 13, 16, 19], [3, 8, 13, 18, 21, 16, 11, 6, 1, 5, 10, 15, 20, 19, 14, 9, 4, 2, 7, 12, 17], [4, 11, 18, 19, 12, 5, 3, 10, 17, 20, 13, 6, 2, 9, 16, 21, 14, 7, 1, 8, 15], [5, 14, 21, 12, 3, 7, 16, 19, 10, 1, 9, 18, 17, 8, 2, 11, 20, 15, 6, 4, 13], [6, 17, 16, 5, 7, 18, 15, 4, 8, 19, 14, 3, 9, 20, 13, 2, 10, 21, 12, 1, 11], [7, 20, 11, 3, 16, 15, 2, 12, 19, 6, 8, 21, 10, 4, 17, 14, 1, 13, 18, 5, 9], [8, 21, 6, 10, 19, 4, 12, 17, 2, 14, 15, 1, 16, 13, 3, 18, 11, 5, 20, 9, 7], [9, 18, 1, 17, 10, 8, 19, 2, 16, 11, 7, 20, 3, 15, 12, 6, 21, 4, 14, 13, 5], [10, 15, 5, 20, 1, 19, 6, 14, 11, 9, 16, 4, 21, 2, 18, 7, 13, 12, 8, 17, 3], [11, 12, 10, 13, 9, 14, 8, 15, 7, 16, 6, 17, 5, 18, 4, 19, 3, 20, 2, 21, 1], [12, 9, 15, 6, 18, 3, 21, 1, 20, 4, 17, 7, 14, 10, 11, 13, 8, 16, 5, 19, 2],

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<group of size 21 with 21 generators>

gap> IsCyclic(last);

true

n=88

gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,13,15,17,19,21,23,25,27,29,31,35,37,39,41,43], [3,9,15,21,27,39,43,37,31,25,19,13,7,1,5,17,23,29,35,41], [5,15,25,35,43,23,13,3,7,17,27,37,41,31,21,1,9,19,29,39], [7,21,35,39,25,3,17,31,43,29,15,1,13,27,41,19,5,9,23,37], [9,27,43,25,7,29,41,23,5,13,31,39,21,3,15,37,19,1,17,35], [13,39,23,3,29,7,19,43,17,9,35,27,1,25,37,15,41,21,5,31], [15,43,13,17,41,19,39,9,21,37,7,23,35,5,25,3,27,31,1,29], [17,37,3,31,23,43,9,25,29,5,39,15,19,35,1,21,13,41,7,27], [19,31,7,43,5,17,21,29,9,41,3,35,15,23,27,39,1,37,13,25], [21,25,17,29,13,9,37,5,41,1,43,3,39,7,35,31,15,27,19,23], [23,19,27,15,31,35,7,39,3,43,1,41,5,37,9,13,29,17,25,21], [25,13,37,1,39,27,23,15,35,3,41,9,29,21,17,5,43,7,31,19], [27,7,41,13,21,1,35,19,15,39,5,29,25,9,43,23,31,3,37,17], [29,1,31,27,3,25,5,35,23,7,37,21,9,39,19,41,17,13,43,15], [31,5,21,41,15,37,25,1,27,35,9,17,43,19,7,29,3,23,39,13], [35,17,1,19,37,15,3,21,39,31,13,5,23,41,29,7,25,43,27,9], [37,23,9,5,19,41,27,13,1,15,29,43,31,17,3,25,39,35,21,7], [39,29,19,9,1,21,31,41,37,27,17,7,3,13,23,43,35,25,15,5], [41,35,29,23,17,5,1,7,13,19,25,31,37,43,39,27,21,15,9,3], [43,41,39,37,35,31,29,27,25,23,21,19,17,15,13,9,7,5,3,1]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20], [2, 5, 7, 10, 13, 18, 20, 17, 15, 12, 9, 6, 4, 1, 3, 8, 11, 14, 16, 19], [3, 7, 12, 16, 20, 11, 6, 2, 4, 8, 13, 17, 19, 15, 10, 1, 5, 9, 14, 18], [4, 10, 16, 18, 12, 2, 8, 15, 20, 14, 7, 1, 6, 13, 19, 9, 3, 5, 11, 17], [5, 13, 20, 12, 4, 14, 19, 11, 3, 6, 15, 18, 10, 2, 7, 17, 9, 1, 8, 16], [6, 18, 11, 2, 14, 4, 9, 20, 8, 5, 16, 13, 1, 12, 17, 7, 19, 10, 3, 15], [7, 20, 6, 8, 19, 9, 18, 5, 10, 17, 4, 11, 16, 3, 12, 2, 13, 15, 1, 14], [8, 17, 2, 15, 11, 20, 5, 12, 14, 3, 18, 7, 9, 16, 1, 10, 6, 19, 4, 13], [9, 15, 4, 20, 3, 8, 10, 14, 5, 19, 2, 16, 7, 11, 13, 18, 1, 17, 6, 12], [10, 12, 8, 14, 6, 5, 17, 3, 19, 1, 20, 2, 18, 4, 16, 15, 7, 13, 9, 11], [11, 9, 13, 7, 15, 16, 4, 18, 2, 20, 1, 19, 3, 17, 5, 6, 14, 8, 12, 10], [12, 6, 17, 1, 18, 13, 11, 7, 16, 2, 19, 5, 14, 10, 8, 3, 20, 4, 15, 9], [13, 4, 19, 6, 10, 1, 16, 9, 7, 18, 3, 14, 12, 5, 20, 11, 15, 2, 17, 8], [14, 1, 15, 13, 2, 12, 3, 16, 11, 4, 17, 10, 5, 18, 9, 19, 8, 6, 20, 7], [15, 3, 10, 19, 7, 17, 12, 1, 13, 16, 5, 8, 20, 9, 4, 14, 2, 11, 18, 6], [16, 8, 1, 9, 17, 7, 2, 10, 18, 15, 6, 3, 11, 19, 14, 4, 12, 20, 13, 5],

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n=90

gap> ct:=CanonicalCayleyTable([[1,7,11,13,17,19,23,29,31,37,41,43], [7,41,13,1,29,43,19,23,37,11,17,31],[11,13,31,37,7,29,17,41,19,43,1,23], [13,1,37,11,41,23,29,17,43,31,7,19],[17,29,7,41,19,37,31,43,13,1,23,11], [19,43,29,23,37,1,13,11,41,17,31,7],[23,19,17,29,31,13,11,37,7,41,43,1], [29,23,41,17,43,11,37,31,1,7,19,13],[31,37,19,43,13,41,7,1,29,23,11,17], [37,11,43,31,1,17,41,7,23,19,13,29],[41,17,1,7,23,31,43,19,11,13,29,37], [43,31,23,19,11,7,1,13,17,29,37,41]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12], [2, 11, 4, 1, 8, 12, 6, 7, 10, 3, 5, 9], [3, 4, 9, 10, 2, 8, 5, 11, 6, 12, 1, 7], [4, 1, 10, 3, 11, 7, 8, 5, 12, 9, 2, 6], [5, 8, 2, 11, 6, 10, 9, 12, 4, 1, 7, 3], [6, 12, 8, 7, 10, 1, 4, 3, 11, 5, 9, 2], [7, 6, 5, 8, 9, 4, 3, 10, 2, 11, 12, 1], [8, 7, 11, 5, 12, 3, 10, 9, 1, 2, 6, 4], [9, 10, 6, 12, 4, 11, 2, 1, 8, 7, 3, 5], [10, 3, 12, 9, 1, 5, 11, 2, 7, 6, 4, 8], [11, 5, 1, 2, 7, 9, 12, 6, 3, 4, 8, 10], [12, 9, 7, 6, 3, 2, 1, 4, 5, 8, 10, 11]] gap> GroupByMultiplicationTable(last); <group of size 12 with 12 generators> gap> IsCyclic(last); true

n=92

gap> ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,19,21,25,27,29,31,33,35,37,39,41,43,45], [3,9,15,21,27,33,39,45,41,35,29,17,11,5,1,7,13,19,25,31,37,43], [5,15,25,35,45,37,27,17,7,3,13,33,43,39,29,19,9,1,11,21,31,41], [7,21,35,43,29,15,1,13,27,41,37,9,5,19,33,45,31,17,3,11,25,39], [9,27,45,29,11,7,25,43,31,13,5,41,33,15,3,21,39,35,17,1,19,37], [11,33,37,15,7,29,41,19,3,25,45,1,21,43,27,5,17,39,31,9,13,35], [13,39,27,1,25,41,15,11,37,29,3,43,17,9,35,31,5,21,45,19,7,33], [15,45,17,13,43,19,11,41,21,9,39,7,37,25,5,35,27,3,33,29,1,31], [17,41,7,27,31,3,37,21,13,45,11,35,1,33,25,9,43,15,19,39,5,29], [19,35,3,41,13,25,29,9,45,7,31,15,39,1,37,17,21,33,5,43,11,27], [21,29,13,37,5,45,3,39,11,31,19,27,15,35,7,43,1,41,9,33,17,25], [25,17,33,9,41,1,43,7,35,15,27,19,31,11,39,3,45,5,37,13,29,21], [27,11,43,5,33,21,17,37,1,39,15,31,7,45,9,29,25,13,41,3,35,19], [29,5,39,19,15,43,9,25,33,1,35,11,45,13,21,37,3,31,27,7,41,17], [31,1,29,33,3,27,35,5,25,37,7,39,9,21,41,11,19,43,13,17,45,15], [33,7,19,45,21,5,31,35,9,17,43,3,29,37,11,15,41,25,1,27,39,13], [35,13,9,31,39,17,5,27,43,21,1,45,25,3,19,41,29,7,15,37,33,11],

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- [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22], [2, 5, 8, 11, 13, 16, 19, 22, 20, 17, 14, 9, 6, 3, 1, 4, 7, 10, 12, 15, 18, 21],
 - [3, 8, 12, 17, 22, 18, 13, 9, 4, 2, 7, 16, 21, 19, 14, 10, 5, 1, 6, 11, 15, 20], [4, 11, 17, 21, 14, 8, 1, 7, 13, 20, 18, 5, 3, 10, 16, 22, 15, 9, 2, 6, 12, 19],
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- [9, 20, 4, 13, 15, 2, 18, 11, 7, 22, 6, 17, 1, 16, 12, 5, 21, 8, 10, 19, 3, 14], [10, 17, 2, 20, 7, 12, 14, 5, 22, 4, 15, 8, 19, 1, 18, 9, 11, 16, 3, 21, 6, 13],
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- [17, 7, 5, 15, 19, 9, 3, 13, 21, 11, 1, 22, 12, 2, 10, 20, 14, 4, 8, 18, 16, 6], [18, 10, 1, 9, 17, 19, 11, 2, 8, 16, 20, 3, 7, 15, 21, 12, 4, 6, 14, 22, 13, 5],
- [19, 12, 6, 2, 9, 15, 22, 16, 10, 3, 5, 18, 20, 13, 7, 1, 8, 14, 21, 17, 11, 4], [20, 15, 11, 6, 1, 5, 10, 14, 19, 21, 16, 7, 2, 4, 9, 13, 18, 22, 17, 12, 8, 3],
- [21, 18, 15, 12, 10, 7, 4, 1, 3, 6, 9, 14, 17, 20, 22, 19, 16, 13, 11, 8, 5, 2], [22, 21, 20, 19, 18, 17, 16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]]
- gap> GroupByMultiplicationTable(last);
- <group of size 22 with 22 generators>
- gap> IsCyclic(last);

```
true
```

```
n=94
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gap>

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ct:=CanonicalCayleyTable([[1,3,5,7,9,11,13,15,17,19,21,23,25,27,29,31,33,35,37,39,41,43,45],
[3,9,15,21,27,33,39,45,43,37,31,25,19,13,7,1,5,11,17,23,29,35,41],
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[7,21,35,45,31,17,3,11,25,39,41,27,13,1,15,29,43,37,23,9,5,19,33],
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[13,39,29,3,23,45,19,7,33,35,9,17,43,25,1,27,41,15,11,37,31,5,21],
```

[15,45,19,11,41,23,7,37,27,3,33,31,1,29,35,5,25,39,9,21,43,13,17], [17,43,9,25,35,1,33,27,7,41,19,15,45,11,23,37,3,31,29,5,39,21,13], [19,37,1,39,17,21,35,3,41,15,23,33,5,43,13,25,31,7,45,11,27,29,9], [21,31,11,41,1,43,9,33,19,23,29,13,39,3,45,7,35,17,25,27,15,37,5], [23,25,21,27,19,29,17,31,15,33,13,35,11,37,9,39,7,41,5,43,3,45,1], [25,19,31,13,37,7,43,1,45,5,39,11,33,17,27,23,21,29,15,35,9,41,3], [27,13,41,1,39,15,25,29,11,43,3,37,17,23,31,9,45,5,35,19,21,33,7], [29,7,43,15,21,37,1,35,23,13,45,9,27,31,5,41,17,19,39,3,33,25,11],[31,1,33,29,3,35,27,5,37,25,7,39,23,9,41,21,11,43,19,13,45,17,15], [33,5,23,43,15,13,41,25,3,31,35,7,21,45,17,11,39,27,1,29,37,9,19], [35,11,13,37,33,9,15,39,31,7,17,41,29,5,19,43,27,3,21,45,25,1,23], [37,17,3,23,43,31,11,9,29,45,25,5,15,35,39,19,1,21,41,33,13,7,27], [39,23,7,9,25,41,37,21,5,11,27,43,35,19,3,13,29,45,33,17,1,15,31], [41,29,17,5,7,19,31,43,39,27,15,3,9,21,33,45,37,25,13,1,11,23,35], [43,35,27,19,11,3,5,13,21,29,37,45,41,33,25,17,9,1,7,15,23,31,39], [45,41,37,33,29,25,21,17,13,9,5,1,3,7,11,15,19,23,27,31,35,39,43]]);

- [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23],
- [2, 5, 8, 11, 14, 17, 20, 23, 22, 19, 16, 13, 10, 7, 4, 1, 3, 6, 9, 12, 15, 18, 21],
- [3, 8, 13, 18, 23, 20, 15, 10, 5, 1, 6, 11, 16, 21, 22, 17, 12, 7, 2, 4, 9, 14, 19],
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- [11, 16, 6, 21, 1, 22, 5, 17, 10, 12, 15, 7, 20, 2, 23, 4, 18, 9, 13, 14, 8, 19, 3], [12, 13, 11, 14, 10, 15, 9, 16, 8, 17, 7, 18, 6, 19, 5, 20, 4, 21, 3, 22, 2, 23, 1],
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- [15, 4, 22, 8, 11, 19, 1, 18, 12, 7, 23, 5, 14, 16, 3, 21, 9, 10, 20, 2, 17, 13, 6], [16, 1, 17, 15, 2, 18, 14, 3, 19, 13, 4, 20, 12, 5, 21, 11, 6, 22, 10, 7, 23, 9, 8],
- [17, 3, 12, 22, 8, 7, 21, 13, 2, 16, 18, 4, 11, 23, 9, 6, 20, 14, 1, 15, 19, 5, 10],
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- [21, 15, 9, 3, 4, 10, 16, 22, 20, 14, 8, 2, 5, 11, 17, 23, 19, 13, 7, 1, 6,

12, 18], [22, 18, 14, 10, 6, 2, 3, 7, 11, 15, 19, 23, 21, 17, 13, 9, 5,

1, 4, 8, 12, 16, 20],

[23, 21, 19, 17, 15, 13, 11, 9, 7, 5, 3, 1, 2, 4, 6, 8, 10, 12, 14, 16, 18,

20, 22]]

gap> GroupByMultiplicationTable(last);

<group of size 23 with 23 generators>

gap> IsCyclic(last);

true

n=96

gap> ct:=CanonicalCayleyTable([[1,5,7,11,13,17,19,23,25,29,31,35,37,41,43,47], [5,25,35,41,31,11,1,19,29,47,37,17,7,13,23,43],[7,35,47,19,5,23,37,31,17,11,25,43,29,1,13,41],[11,41,19,25,47,5,17,35,13,31,43,1,23,29,7,37],[13,31,5,47,23,29,41,11,37,7,19,25,1,43,17,35], [17,11,23,5,29,1,35,7,41,13,47,19,43,25,37,31], [19,1,37,17,41,35,23,43,5,25,13,7,31,11,47,29],[23,19,31,35,11,7,43,47,1,5,41,37,13,17,29,25],[25,29,17,13,37,41,5,1,47,43,7,11,35,31,19,23], [29,47,11,31,7,13,25,5,43,23,35,41,17,37,1,19],[31,37,25,43,19,47,13,41,7,35,1,29,5,23,11,17], [35,17,43,1,25,19,7,37,11,41,29,23,47,5,31,13],[37,7,29,23,1,43,31,13,35,17,5,47,25,19,41,11], [41,13,1,29,43,25,11,17,31,37,23,5,19,47,35,7],[43,23,13,7,17,37,47,29,19,1,11,31,41,35,25,5], [47,43,41,37,35,31,29,25,23,19,17,13,11,7,5,1]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16], [2, 9, 12, 14, 11, 4, 1, 7, 10, 16, 13, 6, 3, 5, 8, 15], [3, 12, 16, 7, 2, 8, 13, 11, 6, 4, 9, 15, 10, 1, 5, 14], [4, 14, 7, 9, 16, 2, 6, 12, 5, 11, 15, 1, 8, 10, 3, 13], [5, 11, 2, 16, 8, 10, 14, 4, 13, 3, 7, 9, 1, 15, 6, 12], [6, 4, 8, 2, 10, 1, 12, 3, 14, 5, 16, 7, 15, 9, 13, 11], [7, 1, 13, 6, 14, 12, 8, 15, 2, 9, 5, 3, 11, 4, 16, 10], [8, 7, 11, 12, 4, 3, 15, 16, 1, 2, 14, 13, 5, 6, 10, 9], [9, 10, 6, 5, 13, 14, 2, 1, 16, 15, 3, 4, 12, 11, 7, 8], [10, 16, 4, 11, 3, 5, 9, 2, 15, 8, 12, 14, 6, 13, 1, 7], [11, 13, 9, 15, 7, 16, 5, 14, 3, 12, 1, 10, 2, 8, 4, 6], [12, 6, 15, 1, 9, 7, 3, 13, 4, 14, 10, 8, 16, 2, 11, 5], [13, 3, 10, 8, 1, 15, 11, 5, 12, 6, 2, 16, 9, 7, 14, 4], [14, 5, 1, 10, 15, 9, 4, 6, 11, 13, 8, 2, 7, 16, 12, 3], [15, 8, 5, 3, 6, 13, 16, 10, 7, 1, 4, 11, 14, 12, 9, 2], [16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]] gap> GroupByMultiplicationTable(last); <group of size 16 with 16 generators> gap> IsCyclic(last); false n=98

gap> ct:=CanonicalCayleyTable([[1,3,5,9,11,13,15,17,19,23,25,27,29,31,33,37,39,41,43,45,47], [3,9,15,27,33,39,45,47,41,29,23,17,11,5,1,13,19,25,31,37,43], [5,15,25,45,43,33,23,13,3,17,27,37,47,41,31,11,1,9,19,29,39], [9,27,45,17,1,19,37,43,25,11,29,47,33,15,3,39,41,23,5,13,31], [11,33,43,1,23,45,31,9,13,41,19,3,25,47,29,15,37,39,17,5,27], [13,39,33,19,45,27,1,25,47,5,31,41,15,11,37,9,17,43,29,3,23], [15,45,23,37,31,1,29,39,9,47,17,13,43,25,5,33,3,27,41,11,19], [17,47,13,43,9,25,39,5,29,1,33,31,3,37,27,41,23,11,45,19,15], [19,41,3,25,13,47,9,29,31,45,15,23,37,1,39,17,43,5,33,27,11], [23,29,17,11,41,5,47,1,45,39,13,33,19,27,25,31,15,37,9,43,3], [25,23,27,29,19,31,17,33,15,13,37,11,39,9,41,43,5,45,3,47,1],

[27,17,37,47,3,41,13,31,23,33,11,43,1,45,9,19,25,29,15,39,5], [29,11,47,33,25,15,43,3,37,19,39,1,41,17,23,5,45,13,27,31,9], [31,5,41,15,47,11,25,37,1,27,9,45,17,19,43,29,33,3,39,23,13], [33,1,31,3,29,37,5,27,39,25,41,9,23,43,11,45,13,19,47,15,17], [37,13,11,39,15,9,33,41,17,31,43,19,5,29,45,3,27,47,23,1,25], [39,19,1,41,37,17,3,23,43,15,5,25,45,33,13,27,47,31,11,9,29], [41,25,9,23,39,43,27,11,5,37,45,29,13,3,19,47,31,15,1,17,33], [43,31,19,5,17,29,41,45,33,9,3,15,27,39,47,23,11,1,13,25,37], [45,37,29,13,5,3,11,19,27,43,47,39,31,23,15,1,9,17,25,33,41], [47,43,39,31,27,23,19,15,11,3,1,5,9,13,17,25,29,33,37,41,45]]); [[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21], [2, 4, 7, 12, 15, 17, 20, 21, 18, 13, 10, 8, 5, 3, 1, 6, 9, 11, 14, 16, 19], [3, 7, 11, 20, 19, 15, 10, 6, 2, 8, 12, 16, 21, 18, 14, 5, 1, 4, 9, 13, 17], [4, 12, 20, 8, 1, 9, 16, 19, 11, 5, 13, 21, 15, 7, 2, 17, 18, 10, 3, 6, 14], [5, 15, 19, 1, 10, 20, 14, 4, 6, 18, 9, 2, 11, 21, 13, 7, 16, 17, 8, 3, 12], [6, 17, 15, 9, 20, 12, 1, 11, 21, 3, 14, 18, 7, 5, 16, 4, 8, 19, 13, 2, 10], [7, 20, 10, 16, 14, 1, 13, 17, 4, 21, 8, 6, 19, 11, 3, 15, 2, 12, 18, 5, 9], [8, 21, 6, 19, 4, 11, 17, 3, 13, 1, 15, 14, 2, 16, 12, 18, 10, 5, 20, 9, 7], [9, 18, 2, 11, 6, 21, 4, 13, 14, 20, 7, 10, 16, 1, 17, 8, 19, 3, 15, 12, 5], [10, 13, 8, 5, 18, 3, 21, 1, 20, 17, 6, 15, 9, 12, 11, 14, 7, 16, 4, 19, 2], [11, 10, 12, 13, 9, 14, 8, 15, 7, 6, 16, 5, 17, 4, 18, 19, 3, 20, 2, 21, 1], [12, 8, 16, 21, 2, 18, 6, 14, 10, 15, 5, 19, 1, 20, 4, 9, 11, 13, 7, 17, 3], [13, 5, 21, 15, 11, 7, 19, 2, 16, 9, 17, 1, 18, 8, 10, 3, 20, 6, 12, 14, 4], [14, 3, 18, 7, 21, 5, 11, 16, 1, 12, 4, 20, 8, 9, 19, 13, 15, 2, 17, 10, 6], [15, 1, 14, 2, 13, 16, 3, 12, 17, 11, 18, 4, 10, 19, 5, 20, 6, 9, 21, 7, 8], [16, 6, 5, 17, 7, 4, 15, 18, 8, 14, 19, 9, 3, 13, 20, 2, 12, 21, 10, 1, 11], [17, 9, 1, 18, 16, 8, 2, 10, 19, 7, 3, 11, 20, 15, 6, 12, 21, 14, 5, 4, 13], [18, 11, 4, 10, 17, 19, 12, 5, 3, 16, 20, 13, 6, 2, 9, 21, 14, 7, 1, 8, 15], [19, 14, 9, 3, 8, 13, 18, 20, 15, 4, 2, 7, 12, 17, 21, 10, 5, 1, 6, 11, 16], [20, 16, 13, 6, 3, 2, 5, 9, 12, 19, 21, 17, 14, 10, 7, 1, 4, 8, 11, 15, 18], [21, 19, 17, 14, 12, 10, 9, 7, 5, 2, 1, 3, 4, 6, 8, 11, 13, 15, 16, 18, 20] 1

gap> GroupByMultiplicationTable(last); <group of size 21 with 21 generators> gap> IsCyclic(last); true

n=100

gap> ct:=CanonicalCayleyTable([[1,3,7,9,11,13,17,19,21,23,27,29,31,33,37,39,41,43,47,49], [3,9,21,27,33,39,49,43,37,31,19,13,7,1,11,17,23,29,41,47], [7,21,49,37,23,9,19,33,47,39,11,3,17,31,41,27,13,1,29,43], [9,27,37,19,1,17,47,29,11,7,43,39,21,3,33,49,31,13,23,41], [11,33,23,1,21,43,13,9,31,47,3,19,41,37,7,29,49,27,17,39], [13,39,9,17,43,31,21,47,27,1,49,23,3,29,19,7,33,41,11,37], [17,49,19,47,13,21,11,23,43,9,41,7,27,39,29,37,3,31,1,33], [19,43,33,29,9,47,23,39,1,37,13,49,11,27,3,41,21,17,7,31], [21,37,47,11,31,27,43,1,41,17,33,9,49,7,23,19,39,3,13,29], [23,31,39,7,47,1,9,37,17,29,21,33,13,41,49,3,43,11,19,27], [27,19,11,43,3,49,41,13,33,21,29,17,37,9,1,47,7,39,31,23], [29,13,3,39,19,23,7,49,9,33,17,41,1,43,27,31,11,47,37,21], [31,7,17,21,41,3,27,11,49,13,37,1,39,23,47,9,29,33,43,19], [33,1,31,3,37,29,39,27,7,41,9,43,23,11,21,13,47,19,49,17],

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true